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# Crystal growth pattern changes in low molecular weight poly(ethylene oxide) ultrathin films

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### ABSTRACT

A low molecular weight (MW) poly(ethylene oxide) (PEO) crystallized in ultrathin films displays various crystal growth patterns in a crystallization temperature ( $T_{\rm X}$ ) range from 20.0 °C to 50.0 °C. In succession, the following patterns are found: nearly one-dimensional (1D) dendrite-like crystal patterns at  $T_{\rm X} \leq 38.0$  °C, two-dimensional (2D) seaweed-like patterns between 39.0 °C  $\leq T_{\rm X} \leq 42.0$  °C and again, nearly 1D dendrite-like patterns at  $T_{\rm X} \geq 43.0$  °C. These transitions result from a complex interplay of varying growth rates along different growth directions and preservation of growth planes. Structural analysis carried out via electron diffraction indicates that the dendrite-like crystals formed at the low and high  $T_{\rm X}$  values differ by their fast growth directions: along the {120} normal at the low  $T_{\rm X}$  values and along the (100) and (010) normal at the high  $T_{\rm X}$  values. In the later case however, the major growth faces are still the {120}, this time tilted at 45° and indicating the  $a^*$  and b axes growth tips. In the intermediate  $T_{\rm X}$  range (39.0 °C–42.0 °C), three growth directions coexist giving rise to the seaweed morphology. The crystal growth rates at the low and high  $T_{\rm X}$  values are constant versus time. For the seaweed, a square-root dependence is obtained. These differences are probably due to 1D and 2D growth in the ultrathin films and are associated with different growth patterns of the dendrites and the seaweed, respectively.

## 1. Introduction

Crystallization of polymers is one of the most intriguing topics in macromolecular physics [1,2]. Due to their long-chain nature, polymer chains kinetically prefer to fold back and forth to form metastable folded-chain lamellar crystals under supercooled conditions [1–4]. The shape of single crystals may change with crystallization conditions (solution, bulk, crystallization temperature ( $T_x$ ), and others) due to the different dependencies of the growth rates of different crystallographic planes. For example, single crystals of polyethylene (PE) show a lozenge or truncated lozenge shape in good solvent and even a lenticular habit in poor solvent at high  $T_x$  [2,5–8]. Toda observed that PE single crystals grown in the bulk change from truncated lozenge to lenticular shape with increasing  $T_x$  [9,10]. Kovacs et al. and Cheng et al. found

that the shape of poly(ethylene oxide) (PEO) single crystals change from a faceted habit to rounded and back to faceted in a  $T_x$  range near the equilibrium melting temperature [11–14].

Recently, polymer crystallization in thin and ultrathin films has attracted increasing attention for both practical and scientific reasons [15-36]. Crystallization in ultrathin films is very different from bulk crystallization. Monolayer 2D lamellar crystals are formed in ultrathin films as opposed to three-dimensional (3D) spherulites in the bulk. Furthermore, different types of crystal shapes (e.g. labyrinthine, dendrite, seaweed, compact and faceted single crystals) have been observed in polymer ultrathin films [16-18,22,23,25,31,32,34,35]. A transition from dendrite to seaweed in PEO ultrathin films has also been observed [16,25,28], although the crystallographic relationship and the underlying reason of the transition are still obscure [36-51]. It is accepted that the differences in growth anisotropy are the origin of the different pattern formations [38,41]. A gradual change in the growth anisotropy may result in a progressive pattern evolution from dendrite to seaweed or from one to another dendrite [25,37,39-45,49,52]. Although theoretical studies have illustrated the pattern selection principle in some aspects of growth kinetics [44,45], the limited set

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of experimental data is still insufficient to obtain a universal morphological diagram based on an in-depth understanding of the origin of pattern selections [17,25,31,32,37,39—42,49,52].

In this work, we describe and analyze a dendrite-seaweed-dendrite crystal evolution in ultrathin films of a low molecular weight (MW) PEO in the  $20.0-50.0\,^{\circ}\text{C}$   $T_{\text{x}}$  range. Atomic force microscopy (AFM) was used to observe crystal morphologies. Transmission electron microscopy (TEM), and more specifically electron diffraction (ED) patterns helped to determine the crystal growth directions and growth planes. Crystal growth rates were measured at different  $T_{\text{x}}$  in order to analyze the formation mechanisms of the dendrite and seaweed crystals. The possible origin of crystal growth pattern evolution is discussed.

## 2. Experimental section

A PEO fraction with weight-average molecular weight  $(\overline{M}_W)$  7.2  $\times$  10<sup>3</sup> g/mol and polydispersity index (PDI) 1.01 was purchased from Polymer Source. The two end groups are a methyl group and a hydroxyl group. Its equilibrium melting temperature is  $T_m^0 = 64.1^{\circ}$ C [53]. A toluene solution of PEO (c = 0.01% w/v) was prepared for film deposition.

Square  $0.8 \times 0.8 \text{ cm}^2$  silicon wafers were treated in Piranha solution of H<sub>2</sub>SO<sub>4</sub> (98%): H<sub>2</sub>O<sub>2</sub> = 3:1 at 120 °C for 30 min to provide a layer of -OH groups on the silicon surface. These substrates were then cleaned in an ultrasonic water bath. The contact angle,  $\theta$ , of water on treated silicon wafer was  $\theta = 8^\circ$ . Silicon monoxide substrates supported by copper grids were purchased from Ted Pella Inc for TEM experiments.

Ultrathin PEO films were prepared by drop-casting the solution onto the silicon wafer or the copper grid supported silicon monoxide. The samples were dried at ambient condition and then treated in vacuum for 12 h. The as-prepared samples were heated to 80.0 °C for 10 min to form a uniform molten layer of 3–4.5 nm thick (measured by AFM). They were then cooled to a preset  $T_{\rm x}$  for isothermal crystallization for 12 h. The samples were then cooled to room temperature for AFM and TEM examination.

Crystal growth patterns were imaged with a hot-stage multimode AFM (Digital Instrumental Nanoscope IV). The tapping mode was used to obtain height and amplitude images. The cantilever force was adjusted to a set-point value of 1.3–1.5 V to limit damage to the sample. The scanning rate was 1.0–1.2 Hz for low-magnification images at a resolution of 512  $\times$  512 pixels/image. Taking advantage of in-situ and real-time observations on polymer crystallization using AFM [54–58], kinetic growth experiments were performed in a  $T_{\rm x}$  range of 34.0 °C  $\leq T_{\rm x} \leq$  50.0 °C. When  $T_{\rm x} <$  34.0 °C, the growth is difficult to track because the AFM tip induces many nuclei around the growing tips. For fast crystal growth kinetics, resolutions of 128  $\times$  128 pixels or 256  $\times$  256 pixels/image and a scanning rate of 1.5 Hz were used.

Crystals were also observed using TEM (Philips Tecnai) at an accelerating voltage of 120 kV. Selected area electron diffraction (SAED) experiments were carried out to determine crystal growth directions and growth planes. The *d*-spacings were calibrated using a TICl standard. Molecular modeling and analysis of the diffraction patterns were performed using the Cerius<sup>2</sup> package of Accelrys.

## 3. Results and discussion

## 3.1. Evolution of crystal patterns with crystallization temperatures

Fig. 1a—f shows six AFM amplitude images of the PEO crystals at  $T_{\rm X}$ 's ranging from 20.0 °C to 49.0 °C. Ribbon-like branches are indicative of the preferred growth directions. Fig. 1a represents a typical dendrite-like crystal formed at  $T_{\rm X}=20.0$  °C with primary,

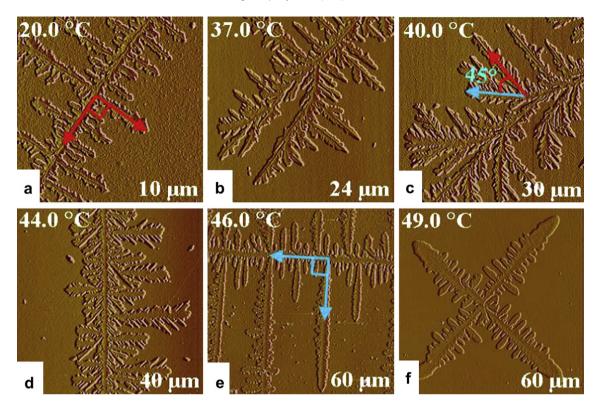
secondary, and sometimes even tertiary branches. These branches possess narrow backbones along the center line (denoted as Bbranches). The angles between the primary and secondary branches or between secondary and tertiary branches are all 90°. The crystals formed at  $T_{\rm X} = 37.0~^{\circ}{\rm C}$  (Fig. 1b) are almost identical to those in Fig. 1a. Yet, some of the branches do not display their recognized backbones along the central line (denoted as NBbranches). The angles between the B- and NB-branches are at 45°. On average, the 90° angle between primary and secondary B-branches is dominant. When crystallization takes place at  $T_{\rm x} = 40.0~^{\circ}{\rm C}$  (Fig. 1c), numerous B- and NB-branches grow alternately and thus, lead to a seaweed-like crystal. Again, the angles between the B- and NB-branches are 45°. At  $T_x = 44.0$  °C (Fig. 1d), the NB-primary branches become the major population with NBsecondary branches. The branching angles between NB-branches are always 90°. B-branches at a 45° angle to the NB-secondary branches exist only in tertiary branches. When increasing  $T_x$  to 46.0 °C (Fig. 1e), a new type of dendrite-like crystal appears. It is only composed of NB-branches with a 90° branching angle. At  $T_x = 49.0$  °C (Fig. 1f), crystals have a typical dendrite-like shape with four branches and approximately a four-fold symmetric structure.

These AFM images illustrate a transition from one type of dendrite crystal to another dendrite type with a seaweed crystal as an intermediate stage with increasing  $T_x$ . The angles between branches of the same kinds (either within the B- or NB-type) are 90°, while those between B- and NB-branches are 45°. Furthermore as shown in Fig. 2, the backbone width in the B-braches is  $T_x$  dependent. At  $T_{\rm x} = 20.0$  °C, the width is ~50 nm, and it increases to  $\sim$  320 nm at 45.0 °C. Fig. 3 shows the thickness  $H_{\rm C}$  of the backbone and the periphery in the B-branches and, the thickness of NBbranches. Backbone thickness increases from 7.2 nm at  $T_x = 20.0 \, ^{\circ}\text{C}$ to 9 nm at  $T_x = 30.0$  °C. The 9 nm value corresponds to a quadruplefolded-chain crystal. The thickness then suddenly increases to 11 nm at  $T_x = 36.0$  °C and further to 15 nm at 43.0 °C, which suggests that the chains fold three and two times, respectively [59]. It should be noted however that the thickness of the backbone in B-branches is generally 1 nm thicker than the periphery until  $T_x = 45.0$  °C. Specifically, these two thickness values are in the non-integral folding stage at lower  $T_X$  and increase in a quantized fashion based on integral folding at higher T<sub>x</sub>. Beyond 46.0 °C, the B-branches disappear, and the dendrites are only composed of NB-branches. The NBbranch thickness reaches 15 nm (twice-folded integral chains). Further increase to  $T_x = 50.0$  °C leads to a substantial increase of the thickness, indicating that the number of folds decreases, although the  $H_{\rm C}$  value does not yet reach the expected extended chain length.

Upon analysis of the crystal growth patterns of dendrites and seaweeds and the determination of backbone and lamellae thickness, it appears that we are dealing with a complex growth pattern. The crystal growth kinetics in ultrathin films depend on diffusion of crystallizable molecules as well as on the tendency of PEO chains to crystallize in integrally quantized stem lengths that are two, three and four times smaller than the chain length. Only for fast growth rates, especially for  $T_{\rm X} < 30.0~{\rm ^{\circ}C}$ , are the PEO chains in the crystal non-integrally folded [59,60].

## 3.2. Crystal growth directions

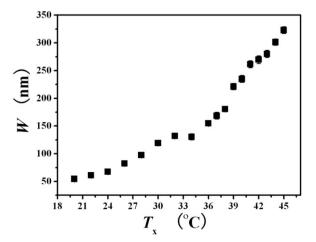
The PEO crystal structure and chain conformation are well known (Fig. 4a): four distorted  $7_2$  helical molecules are packed in a monoclinic unit cell, a=0.805 nm, b=1.304 nm, c=1.948 nm and  $\beta=125.4^\circ$  [61]. It turns out that  $a\times\sin\beta=0.656$  nm is only nearly half of the b dimension in the c axis projection. In most (but not all) growth processes, therefore, the PEO crystal lies on an apparent tetragonal projection. Prominent crystallographic planes are thus  $90^\circ$  apart, e.g. (120) and (1 $\overline{2}0$ ), or (100) and (010). This explains the nearly square



**Fig. 1.** A set of AFM amplitude images showing crystal growth pattern evolution as a function of  $T_x$ . Red and blue arrows represent B-branches and NB-branches respectively, and the angles between them are  $90^{\circ}$  or  $45^{\circ}$ . (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article).

shape of solution grown crystals, and the existence of branches at  $90^{\circ}$  in dendrite growth. Because of this apparent high symmetry, it is not possible to determine the crystallographic axes in the dendrite on morphological outline alone. Such a determination requires, in this case, SAED. Fig. 4b shows the calculated (hk0) diffraction pattern of PEO from the Cerius<sup>2</sup> model. The four strongest diffractions correspond to densely packed (120) planes. The six weaker spots close to the center help to determine  $a^*$  and b axes. We expect that the observed angle selections between branches should be related to the growth directions along the <120>, the  $a^*$  and b axes [28,62,63].

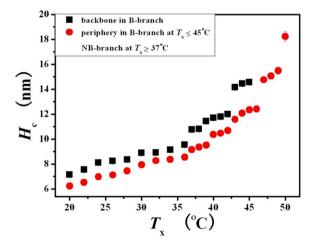
The SAED patterns in correct orientation to the dendrite and seaweed crystals are shown in Fig. 5a. Analysis of the figures reveals the essential difference between the dendrites grown at the low and the high  $T_{\rm x}$  values, in spite of their similar morphologies. In the low  $T_{\rm x}$  dendrites, the branches are parallel to the <120>, whereas for high  $T_{\rm x}$ , the branches are extended along the  $a^*$  and b axes



**Fig. 2.** Width (W) of the backbone in B-branches as a function of  $T_x$ .

(compare the dendrites at  $T_{\rm x}=26.0\,^{\circ}{\rm C}$  and  $46.0\,^{\circ}{\rm C}$ ). In other words, the major growth directions are 45° away for the low and high  $T_{\rm x}$  dendrites. Dendrites composed of B-branches are denoted DB<sub>(120)</sub>, while dendrites composed of NB-branches are denoted DNB<sub>(100)</sub>/<sub>(010)</sub>. At intermediate  $T_{\rm x}$ , between 38.0 °C and 43.0 °C, three growth directions coexist. They give rise to more ill defined morphologies, with curved growth faces, characteristic of the seaweed patterns, although they yield clear single crystal ED patterns. Note however that  $a^*$  and b axes can be differentiated only via SAED experiments.

To summarize the morphological transition of the PEO crystals, three  $T_{\rm x}$  regions are obtained as follows (Fig. 5b): At  $T_{\rm x} \leq$  38.0 °C, DB<sub>(120)</sub> dendrites with a backbone in preferential growth directions



**Fig. 3.** Thickness ( $H_c$ ) of crystal as a function of  $T_x$ . ■ represents the thickness of backbone in B-branch. ● represents the thickness of the periphery in the B-branch at  $T_x \le 45.0$  °C and the thickness of the NB-branch at  $T_x \ge 37.0$  °C. In the region 37.0 °C  $\le T_x \le 45.0$  °C, the thickness of the periphery in the B-branch is equal to the thickness of the NB-branch.

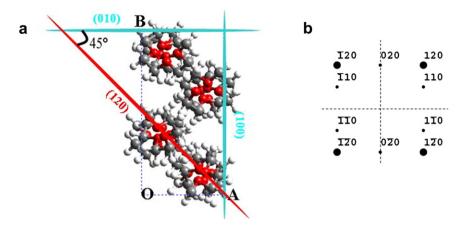


Fig. 4. (a) Unit cell of PEO crystal in the direction of c axis. The angle between the {120} and the (100) or (010) planes is 45°. (b) Calculated [001] zone ED pattern.

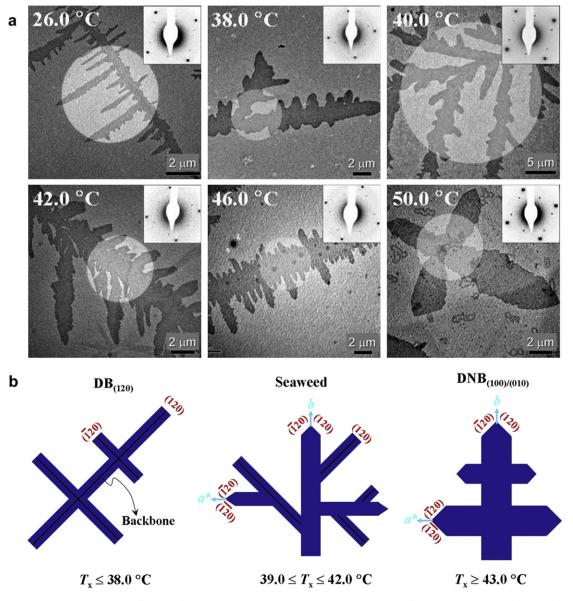


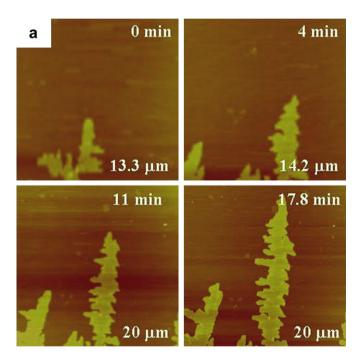
Fig. 5. (a) TEM images and SAED patterns at different  $T_x$ . (b) Schematics showing crystal growth direction changing from the <120> to  $a^*$  and b axes with increasing  $T_x$ .

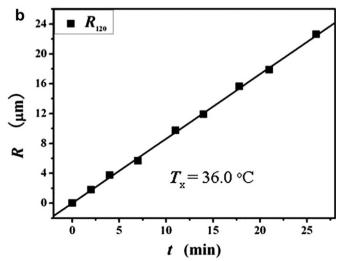
along the <120> and a 90° branching angle; at 39.0 °C  $\leq T_{\rm X} \leq$  42.0 °C, seaweed with growth direction along the <120> and the  $a^*$  and b axes and a 45° branching angle; at  $T_{\rm X} \geq$  43.0 °C, DB<sub>(100)/(010)</sub> dendrites with preferential growth direction along the  $a^*$  and b axes and a 90° branching angle.

## 3.3. Crystal growth rate and mechanisms

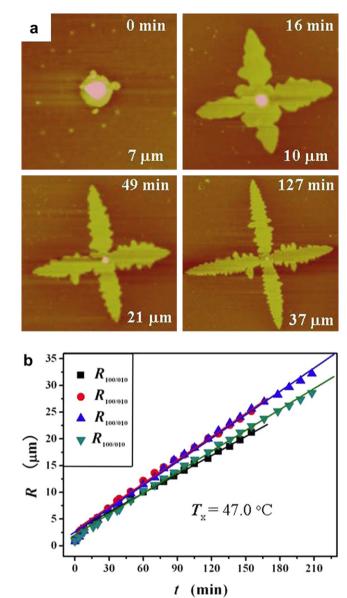
In-situ experiments were performed using AFM to determine the crystal growth rates. AFM is useful in the high  $T_{\rm x}$  range since homogeneous nucleation is difficult in this  $T_{\rm x}$  region, while the AFM tip can induce the crystal nucleation. The results indicate a significant difference between the growth rate time dependencies of both the low and high  $T_{\rm x}$  dendrites on one side and seaweed on the other.

For the dendrites in both temperature regions of  $T_{\rm X} \le 38.0\,^{\circ}{\rm C}$  and  $T_{\rm X} \ge 43.0\,^{\circ}{\rm C}$ , the length of the primary branches, R, along the <120> and the  $a^*$  and b axes are linearly proportional to time (t) as shown in Figs. 6 and 7. This means that dendrite growth rate, G, is a constant





**Fig. 6.** (a) AFM height images present crystal growth as a function of t at  $T_x = 36.0$  °C. (b) Plot of R versus t.  $R_{120}$  represents the length of the B-branch along <120>.

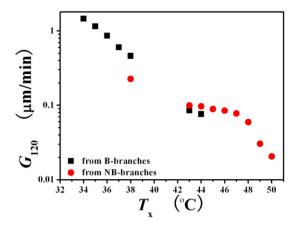


**Fig. 7.** (a) AFM height images present crystal growth as a function of t at  $T_x = 47.0 \,^{\circ}$ C. (b) Plots of R versus t.  $R_{100/010}$  represents the length of the NB-branch along  $a^*$  and b axes.

with respect to t. Fig. 8 shows the growth rate obtained for both the low and high  $T_{\rm x}$  dendrites. The figure illustrates the expected rapid decrease of G with increasing  $T_{\rm x}$  in the low  $T_{\rm x}$  range. In 43.0 °C  $\leq T_{\rm x} \leq$  47.0 °C region however, G remains nearly a constant before decreasing again rapidly when  $T_{\rm x} \geq$  48.0 °C. The overall curve of G versus  $T_{\rm x}$  is strongly reminiscent of plots obtained for similar MW PEO isothermal crystallization from the bulk. In the transition region from integral fold number n to a longer stem length corresponding to n-1 folds, similar growth rate variations have indeed been observed [13,14]. However, the growth mechanism is diffusion-limited in our case versus nucleation-limited in the bulk.

For the seaweeds in the range 39.0 °C  $\leq T_x \leq$  42.0 °C missing in Fig. 8, G is not constant for these entities. Fig. 9 illustrates the growth of the seaweeds and the crystal size R plotted as a function of t and  $t^{1/2}$ . The slope of the R versus t curve decreases with increasing t, which indicates that G continuously decreases with respect to t. On the other hand, R is linearly proportional to  $t^{1/2}$ .

It is known that the formations of both the dendrite and seaweed crystals are controlled by a diffusion-limited mechanism.



**Fig. 8.** Plots of  $G_{120}$  versus  $T_x$ . ■ represents the  $G_{120}$  directly measured from B-branches along <120>. ● represents the  $G_{120}$  derived from the growth rate of NB-branches along  $a^*$  and b axes,  $G_{100/010}$ , where  $G_{120} = (\sqrt{2}/2)G_{100/010}$ . In the seaweed-like crystal region of  $T_x = 39.0 \,^{\circ}\text{C} - 42.0 \,^{\circ}\text{C}$ , the growth rate is not plotted as it is not constant versus t.

Why then should we observe a linear growth versus t in the dendrites and a linear growth versus  $t^{1/2}$  in the seaweeds? Let us first point out that our observation of linear growth versus t is consistent with earlier observations on other dendrite systems [20,64–67], but no clear explanation has been proposed so far. In the following, we attempt to provide a possible explanation.

The linear growth may be explained by the following reasoning and schematic illustrations in Fig. 10. The primary branch in the dendrite is actually a quasi-1D object. Each individual growth tip is surrounded by a local supercooled PEO diffusion field. The growth of a dendrite branch generates a quasi-1D depletion zone parallel to the growth direction of the primary branch. The material transformation from supercooled melt to crystal implies  $dm_{\rm c}=-dm_{\rm a}$ , where  $m_{\rm c}$  and  $m_{\rm a}$  represent the masses of crystal and supercooled melt, respectively. According to Fick's first law and diffusion controlled growth in quasi-1D case,

$$\frac{\partial(\rho_{c}W_{c}H_{c}R)}{\partial t} = W_{a} \times D\frac{\partial\phi_{a}}{\partial x}$$
 (1)

where  $\rho_c$  is the density of the crystal;  $W_c$  is the width of the quasi-1D crystal;  $H_c$  is the height of the crystal; R is the length of the crystal;  $W_a$  is the width of the depletion zone;  $\varphi_a$  represents the mass of the supercooled melt per unit area; and x is the distance from the crystal tip to a specific site ahead of the tip. Because  $\rho_c$ ,  $W_c$ ,  $H_c$ , and  $W_a$  are all constants at a specific  $T_x$ , we have

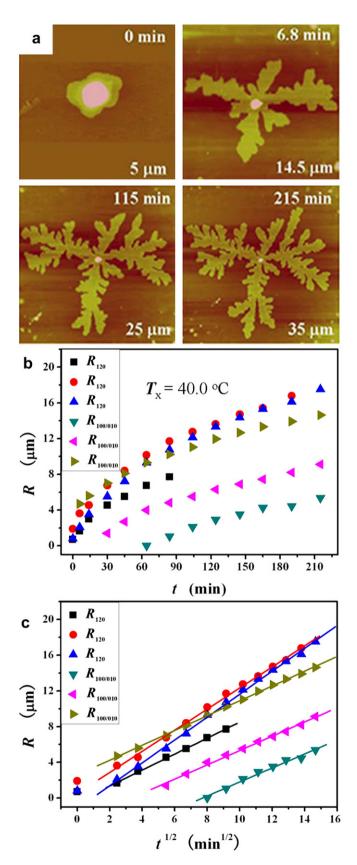
$$\rho_{c}W_{c}H_{c}\frac{\partial R}{\partial t} = DW_{a}\frac{\partial \phi_{a}}{\partial x} \tag{2}$$

then,

$$\frac{\partial R}{\partial t} = (DW_{\rm a}/\rho_{\rm c}W_{\rm c}H_{\rm c})\frac{\partial \phi_{\rm a}}{\partial x} \tag{3}$$

where  $\frac{\partial \phi_a}{\partial x}$  represents the supercooled melt gradient ahead of the crystal tip. At steady state,  $\frac{\partial \phi_a}{\partial x}$  is constant, and therefore, R is linearly proportional to t. This may explain why we observe the linear growth versus t even though the growth is diffusion-limited. This analysis may also provide a possible interpretation for similar observations reported in earlier works [20,64–67].

For the seaweeds, simultaneous growths of B- and NB-branches generate a 2D entity. This leads to the observation that their growths are linearly proportional to  $t^{1/2}$ . The mathematic analysis for this type of 2D growth was made in Ref. [29]. Therefore, the time-dependent change of growth rate from the dendrite to the seaweed is due to growth dimension change, rather than change of the growth mechanism.



**Fig. 9.** (a) AFM height images present crystal growth as a function of t at  $T_{\rm x}=40.0\,^{\circ}{\rm C}$ . (b) Plots of R versus t. (c) Plots of R versus  $t^{1/2}$ .  $R_{120}$  represents the length of the B-branch along <120>, and  $R_{100/010}$  represents the length of the NB-branch along  $a^*$  and b axes.

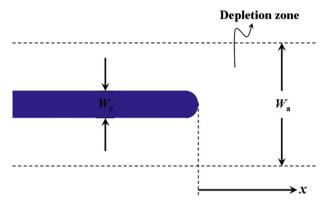


Fig. 10. Schematic illustration of 1D dendrite growth (top view).

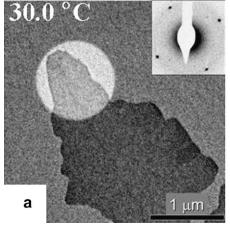
## 3.4. Origin of the crystal pattern change

As illustrated in Fig. 5, the preferential crystal growth direction is along the <120 > at  $T_{\rm x} \leq 38.0~{\rm C}$  and along the  $a^*$  and b axes at  $T_{\rm x} \geq 43.0~{\rm C}$ . Why does the fastest crystal growth direction change in these two  $T_{\rm x}$  regions? Note that in the seaweed-like crystals grown at 39.0 °C  $\leq T_{\rm x} \leq 42.0~{\rm C}$ , three growth directions prevail. Let us analyze the growth tips of the B-branch at  $T_{\rm x} \leq 38.0~{\rm C}$  and NB-branch at  $T_{\rm x} \geq 43.0~{\rm C}$ . For the B-branches in DB<sub>(120)</sub> (Fig. 11a), the tips are flat, and correspond to the {120} planes as indicated by the SAED pattern. For the NB-branch in DNB<sub>(100)/(010)</sub>, although the angle between two {120} planes is smaller than 90° as shown in Fig. 11b (see below for reason), the primary NB-branch grows along the merged corner of the two {120} planes. Therefore, the crystal growth planes remain the same in the entire  $T_{\rm x}$  region, although the fastest growth directions are different.

In the high  $T_{\rm x}$  region above 43.0 °C, the crystal growth mechanism is diffusion-limited [29]. For the diffusion coefficient, D, of PEO chains in ultrathin films, Bi et al. reported  $D=0.6\times 10^{-14}~{\rm m}^2/{\rm s}$  for a PEO with MW =  $5.0\times 10^3$  g/mol in the depleted zone on the surface of  $-{\rm OH}$  decorated glass (that is similar to the surface of  $-{\rm OH}$  decorated silicon wafer in our experiments) at 45.0 °C [68]. Based on the molecular weight dependence [69], the D value for the present PEO is  $4.16\times 10^{-15}~{\rm m}^2/{\rm s}$ , or  $0.25~{\rm \mu m}^2/{\rm min}$ . The PEO growth rate, G, in the high  $T_{\rm x}$  region is around  $0.1-0.01~{\rm \mu m}/{\rm min}$ . Since G and D are comparable, a materials gradient is expected at the growth front. In turn, this speeds up the growth of the crystal tip (the  $a^*$  and b axes), although the growth planes remain the {120} planes. This leads to an angle between two {120} planes smaller than 90° (Fig. 11b). As a result, the DNB $_{(100)/(010)}$  dendrites form in this  $T_{\rm x}$  region.

Next, what is the origin of the DB<sub>(120)</sub> dendrites formed in the region  $T_x \le 38.0$  °C? We speculate that it is because of the preferential fast growth along the <120> direction with a narrow backbone width at the  $\{120\}$  growth face. In this  $T_X$  region, G is much larger than D, so the crystal growth is close to the case of diffusion-limited aggregation [64]. This type of dendrite growth may rely on the fact that the primary nuclei developed in the PEO with a very small size are bounded by {120} planes. The Hoffman-Lauritzen theory predicts that when the crystal growth substrate length is smaller than a critical value that has been responsible for one nucleus and a few hundred nanometers, the growth rate along the substrate normal is faster than the growth rate after the substrate width exceeds this critical value [2,70]. One recent experimental observation has shown that the lateral spread extent increases with  $T_x$  on a length scale between 30 nm and 60 nm in single crystals of a specific polymer [71]. As shown in Fig. 2, the width of the backbone in B-branch increases with  $T_x$ , while their absolute values range from  $\sim 50$  nm at  $T_x = 20.0$  °C to  $\sim$  320 nm at  $T_x = 45.0$  °C. These width values are expected to be close to but smaller than the upper-limit of the critical substrate width at each  $T_{\rm X}$  for the PEO crystal. The narrow backbone width at the growth front leads to a fast growth along the <120> directions, which results in the DB<sub>(120)</sub> dendrites in the region  $T_X \le 38.0$  °C.

The final question is: what are the origins of forming the B- and NB-branches? It is noted that although both growth planes are the {120} planes, the B-branches can form only when the <120> is the fastest growth direction for constructing the frames of the  $DB_{(120)}$ dendrite, while the NB-branches possess a favorable growth direction along the  $a^*$  and b axes forming the DNB<sub>(100)/(010)</sub> dendrite. Above  $T_{\rm x}=30.0$  °C, the backbones in the B-branch are more or less integrally folded-chain crystals. This indicates that the backbones are formed first with certain rearrangements resulting in integral chain crystals. Only below  $T_x = 30.0$  °C can non-integral folded crystals be stabilized. It is worth mentioning that backbones in the B-branches are about 1 nm thicker than the periphery (Fig. 3). During the formation process (Fig. 6a), the thicker backbones always form ahead of the periphery, which is similar to the observation on a similar MW PEO at high  $T_x$  values [11,12]. Other parts of the crystals epitaxially grow on the backbones in the later stages with about a 1 nm thickness decrease. The thinner part may not be able to further reorganize since there is an exhausting of PEO molecules. Any thickening process would generate holes in the crystals and thus, increase the free energy and destabilize the crystals [72]. On the other hand, the NB-branches are developed from a PEO single crystal and grow along the  $a^*$  and b axes, whose tips are composed of two {120} planes. Therefore, the thickness of these two sectors of one single crystal is identical.



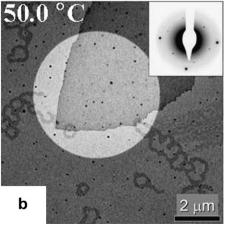


Fig. 11. (a) TEM image and SAED pattern of a B-branch tip at 30.0 °C. (b) TEM image and SAED pattern of an NB-branch tip at  $T_x = 50.0$  °C.

Before concluding, it is useful to compare the present results with earlier reports on similar transitions between dendrite and seaweed type crystals. First, it must be noted that no SAED experiments were performed and therefore the crystal growth directions could not be identified [16,25,28]. As a rule, the PEO film thickness was larger or significantly larger than the crystal thickness. Also, the branching angles in seaweed crystals did not have a fixed value. Therefore, the origin of crystal growth transition was not clearly identified. In this work, the PEO film thickness is smaller than the crystal thickness. The crystal growth patterns are therefore strongly dependent on molecular diffusion. The combination of SAED analyses and crystal growth kinetics reveal that the crystal growth transitions between dendrites and seaweed result from a complex interplay of crystallographic aspects and growth mechanisms.

## 4. Conclusion

We have observed and analyzed  $T_x$ -dependent crystal growth patterns in a low MW PEO in ultrathin films. SAED results indicate that when  $T_x \le 38.0$  °C, dendritic crystals are formed with branches elongated along the <120> directions. Above  $T_X = 43.0$  °C, dendritic crystals are also formed, but the growth directions are along the  $a^*$  or *b* axes. In the intermediate  $T_x$  range, 39.0 °C  $\leq T_x \leq$  42.0 °C, seaweed crystals are observed, in which three growth directions coexist ( $a^*$ , b and <120>). We consider that the crystal growth mechanism in the entire  $T_x$  region is a diffusion-limited process, although the crystal growth rates differ for dendrites and seaweeds because of their different growth geometries. Linear crystal growth rates are observed when  $T_x$  < 38.0 °C and  $T_x$  > 43.0 °C due to the 1D growth geometry of the dendrites. In the intermediate  $T_x$  region where the seaweed crystals are formed, the crystal growth is linearly proportional to  $t^{1/2}$  due to the 2D growth geometry. The origin of dendrite crystals in both low and high  $T_x$  regions is also discussed. It is suggested that at  $T_x \le 38.0$  °C, the growth is close to diffusion-limited aggregation, and the 1D growth may be due to the fact that the substrate width of the growth front is smaller than the critical value of the nucleation event. On the other hand, in the  $T_x \ge 43.0$  °C region, the material gradient near the growth front generates an increase of crystal tip growth leading to the formation of dendrites with branches elongated in the  $a^*$  and b axes directions.

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